

# A Simplified Method for Determining the Bearing Capacity of Eccentrically Compressed Rectangular CFST Columns with Eccentricities in Two Planes



Samir Al-Zgul<sup>1</sup>, Vasilina Tyurina<sup>1</sup>  and Anton Chepurnenko<sup>1,\*</sup> 

<sup>1</sup>Structural Mechanics and Theory of Structures Department, Don State Technical University, Rostov-on-Don, Russia

## Abstract:

**Introduction:** Rectangular concrete-filled steel tubular (CFST) columns are among the most promising types of load-bearing structures. Compared to circular CFST columns, they are more effective in resisting eccentric compression. Existing analytical calculation methods enable the determination of the bearing capacity of eccentrically compressed CFST columns in the presence of axial force eccentricity in only one plane. The purpose of this work is to develop an analytical method for calculating the bearing capacity of eccentrically compressed CFST columns in the presence of bending moments in two planes.

**Materials and Methods:** The proposed model is based on the theory of limit equilibrium. Four main variants of the neutral line location in the cross-section at the moment of destruction are identified. For each variant, resolving equations are obtained that allow for determining the ultimate load, which can be solved using the publicly available Microsoft Excel Online software.

**Results:** The developed method was tested on experimental data for 38 samples. The correlation coefficient between the experimental and calculated values was 0.979. There is also good agreement between the results of analytical calculations and the results of finite element modeling.

**Discussion:** The deviation of the experimental ultimate load values from the calculated ones can be attributed to the scatter of experimental data and the local loss of stability effects on the pipe wall.

**Conclusion:** Engineers can use the proposed method for a preliminary assessment of the bearing capacity for eccentrically compressed CFST columns at the stage of selecting design solutions.

**Keywords:** Concrete-filled steel tubular columns, Load-bearing capacity, Limit equilibrium, Eccentric compression, Eccentricity, Compressive strength.

© 2025 The Author(s). Published by Bentham Open.

This is an open access article distributed under the terms of the Creative Commons Attribution 4.0 International Public License (CC-BY 4.0), a copy of which is available at: <https://creativecommons.org/licenses/by/4.0/legalcode>. This license permits unrestricted use, distribution, and reproduction in any medium, provided the original author and source are credited.

\*Address correspondence to this author at the Structural Mechanics and Theory of Structures Department, Don State Technical University, Rostov-on-Don, Russia; E-mail: [anton\\_chepurnenk@mail.ru](mailto:anton_chepurnenk@mail.ru)

Cite as: Al-Zgul S, Tyurina V, Chepurnenko A. A Simplified Method for Determining the Bearing Capacity of Eccentrically Compressed Rectangular CFST Columns with Eccentricities in Two Planes. Open Constr Build Technol J, 2025; 19: e18748368402845. <http://dx.doi.org/10.2174/0118748368402845250709060829>



CrossMark

Received: April 09, 2025

Revised: April 24, 2025

Accepted: May 06, 2025

Published: July 11, 2025



Send Orders for Reprints to  
[reprints@benthamscience.net](mailto:reprints@benthamscience.net)

## 1. INTRODUCTION

Concrete-filled steel tubular (CFST) columns are widely used in construction due to their high load-bearing capacity, seismic resistance, and cost-effectiveness. Their key advantage is the synergy of the steel shell and concrete core: steel provides ductility and tensile strength, while concrete demonstrates increased compressive strength [1]. This combination increases the load-bearing capacity and gives the columns pronounced dissipative properties, which is critically important for seismically hazardous regions [2-4].

Additional advantages of CFST columns include fire resistance, durability, and the ability to create slender structures without losing strength [5-8]. This is why CFST columns have become a popular choice for high-rise buildings, bridges, and other critical structures worldwide [9].

In their research, scientists consider issues of strength, deformability, and stability of CFST columns under central and eccentric compression, as well as under temperature loads, using experimental, numerical, and normative-analytical calculation methods [10].

Experimental studies, despite their high reliability, require significant financial and time resources, which limits their large-scale application. Since the first experiments conducted by Klöppel and Goder, numerous experimental studies of CFST columns with varying geometric and physical-mechanical characteristics have been carried out, primarily under axial loading, and less frequently under eccentric compression in a single plane [11-25]. The authors compare the experimental results with calculations using national standard methods. An analysis of 3103 CFST column tests previously showed that European

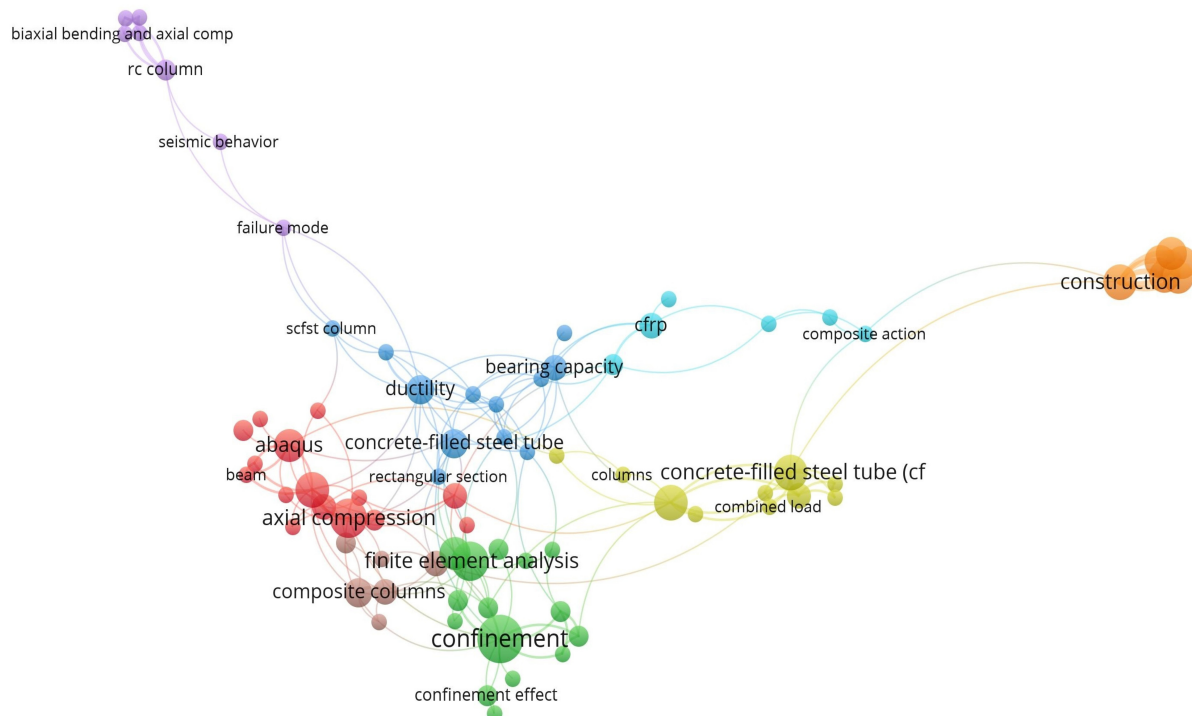
and Australian standards provide more accurate but conservative predictions [26]. However, their application beyond the established limits leads to less reliable results. Du *et al.* note that there are no experimental data available for rectangular columns made of high-strength steels with a yield strength exceeding 400 MPa, which necessitates additional research [27].

Despite the significant volume of experimental data, their fragmentation and lack of systematization make complex analysis and practical application difficult. Additionally, the limitations of testing equipment and the increase in construction scale do not allow for obtaining completely reliable results under various types of loading.

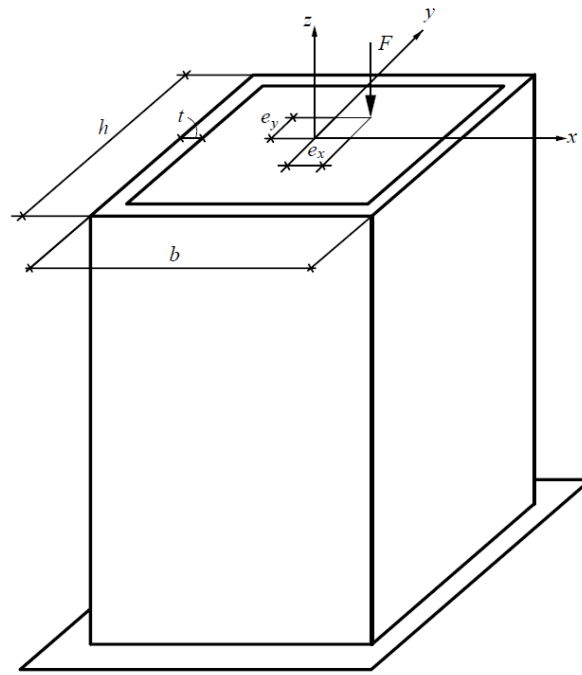
Numerical methods, particularly the finite element method, are widely employed to analyze the behavior of rectangular CFST columns, offering accurate modeling of nonlinear material properties, geometry, and contacts, as well as the impact of concrete lateral compression. The reliability of the obtained results is confirmed by the authors in papers, where the results correlate with calculations using standard methods [28-33].

Compared to circular columns, rectangular columns offer better coupling with beams under complex loading, demonstrating resistance to cyclic loads, which is particularly important in seismically hazardous regions [34, 35].

There are relatively few studies devoted to the analysis of eccentric compression with eccentricities in two planes for rectangular columns, as confirmed by a bibliometric network analysis of 783 scientific sources using VOSviewer software (Fig. 1) [36]. Most works consider CFST columns with compression and bending only in one plane.



**Fig. (1).** Bibliometric map of CFST column research.



**Fig. (2).** Calculation scheme.

Visualization of the key research areas thematic network revealed understudied areas, particularly the area of eccentric compression with eccentricities in two planes (biaxial bending and axial compression), which is represented on the knowledge map by a small cluster weakly connected to the main areas. This suggests that research in this area is being conducted, but its integration into the overall scientific agenda is limited: the main focus is on numerical analysis methods, while analytical models that take into account biaxial loading are practically under-represented.

The conducted literature analysis confirms the relevance of the study, which aims to develop methods for assessing the strength of CFST columns operating under complex stress conditions. The purpose of this work is to develop a simplified analytical method for calculating the bearing capacity of eccentrically compressed CFST columns in the combined action of axial forces and biaxial bending. Such a method will allow engineers to obtain quick and well-founded solutions without the need to develop complex calculation models in software packages or perform labor-intensive experimental studies.

The article is structured as follows. The materials and methods section presents the main assumptions of the model, possible failure schemes, and the resolving equations for each scheme. The results and discussion section presents the testing of the proposed model using experimental data. A numerical example of calculation is also presented to enable the reproduction of the results by other researchers. In conclusion, the main findings of the work are presented.

## 2. MATERIALS AND METHODS

The calculation scheme of the considered structure, which is an eccentrically compressed rectangular CFST column experiencing compression with biaxial bending, is shown in Fig. (2).

The simplified method is based on the following assumptions:

1. The increase in compressive strength of concrete in a CFST element due to the effect of lateral compression is not taken into account.
2. The stress in the compressed zone of the concrete core in the limit state is constant and equal to the compressive strength of concrete  $R_b$ .
3. The stresses in the tensile zone of the concrete core are neglected.
4. The material of the steel shell is assumed to be ideal elastic-plastic, and in the limit state, the stresses in the tensile and compressed zones of the steel shell are equal to the yield strength of the steel  $R_y$  with the corresponding sign.
5. The neutral line, which divides the section into compressed and stretched zones, is the straight line in the limit state.
6. The dimensions of the concrete core are assumed to be approximately equal to the external dimensions of the column cross-section. That is, the wall thickness of the rectangular steel profile pipe is considered negligible compared to the cross-section dimensions.
7. The effects of local stability loss due to the pipe wall are neglected.

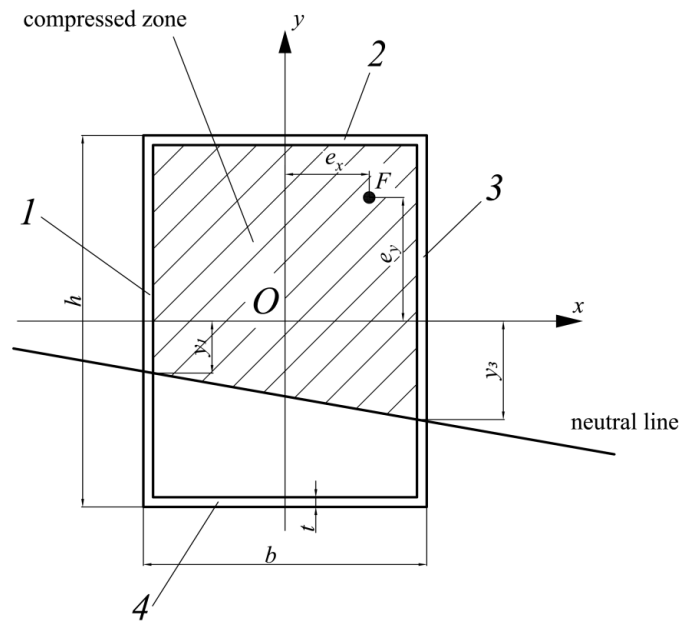
8. Additional eccentricities of the axial force caused by the deflection of the element are not taken into account.

Assumptions 2-5 are the standard hypotheses of the limit equilibrium method [37]. Hypothesis 8 implies that geometric nonlinearity is not considered in the calculation. Its consideration is well developed for the case of bending in one plane [38], but for biaxial bending, its consideration in the analytical model will cause great difficulties.

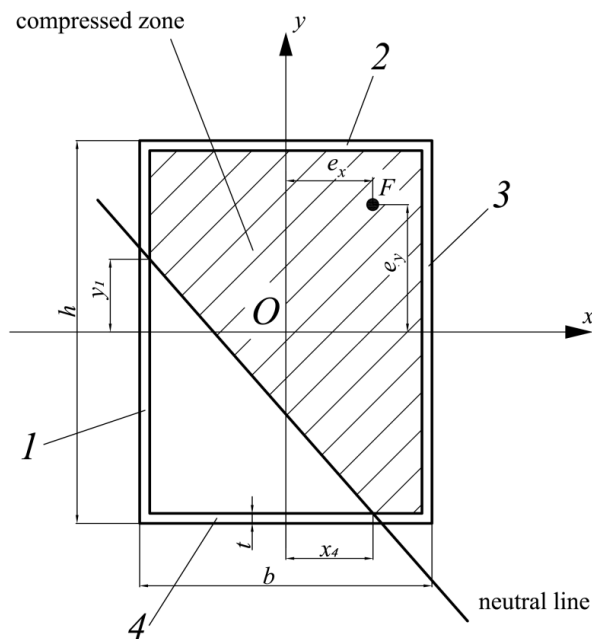
For convenience, we will assume that the point of application of the eccentric compressive force is located in the first quadrant of the coordinate system  $xOy$ . Depending on the relationship between the eccentricities of the axial force  $e_x, e_y$ , seven cases are possible:

1) The neutral line intersects sides 1 and 3 of the cross-section contour (Fig. 3).

2) The neutral line intersects sides 1 and 4 of the cross-section contour (Fig. 4).



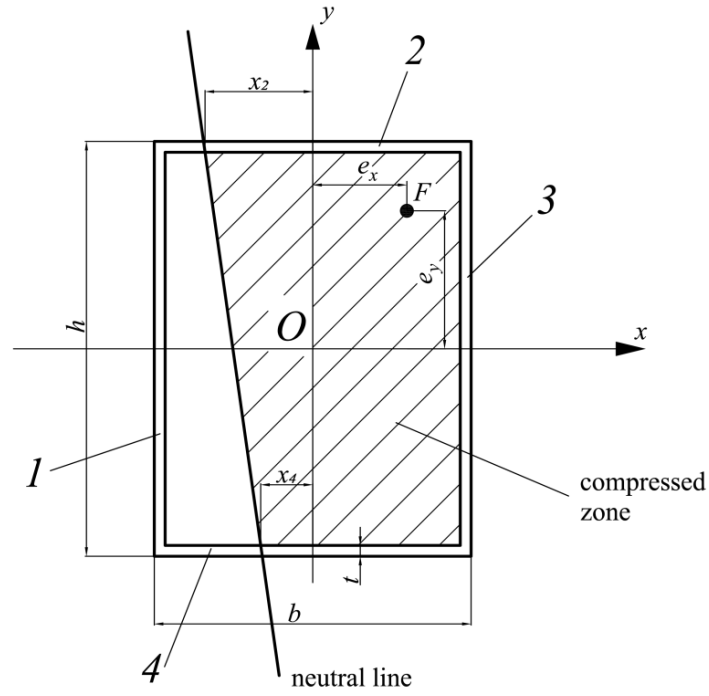
**Fig. (3).** Option 1 of the neutral line position.



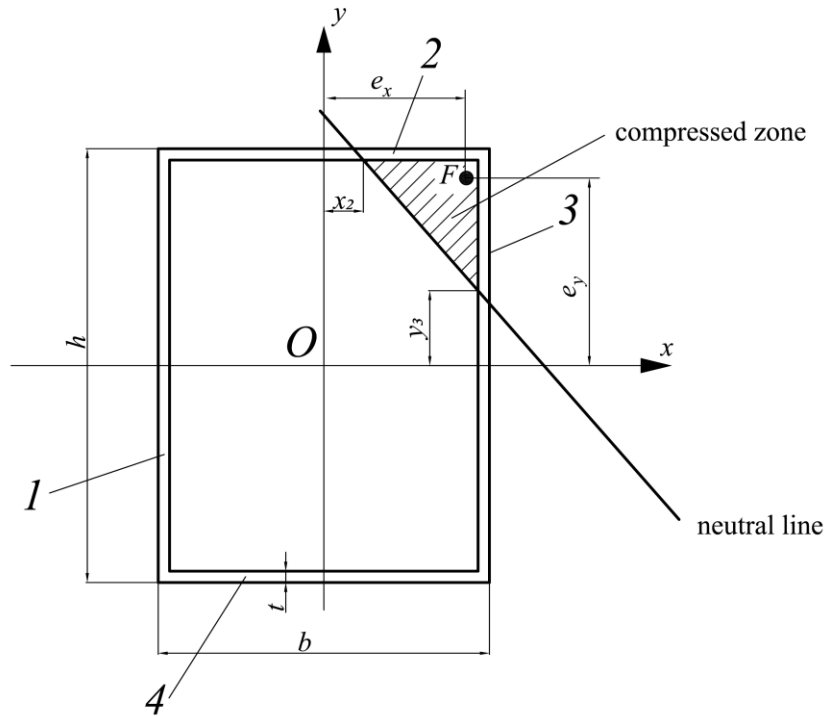
**Fig. (4).** Option 2 of the neutral line position.

3) The neutral line intersects sides 2 and 4 of the cross-section contour (Fig. 5).

4) The neutral line intersects sides 2 and 3 of the cross-section contour (Fig. 6).



**Fig. (5).** Option 3 of the neutral line position.

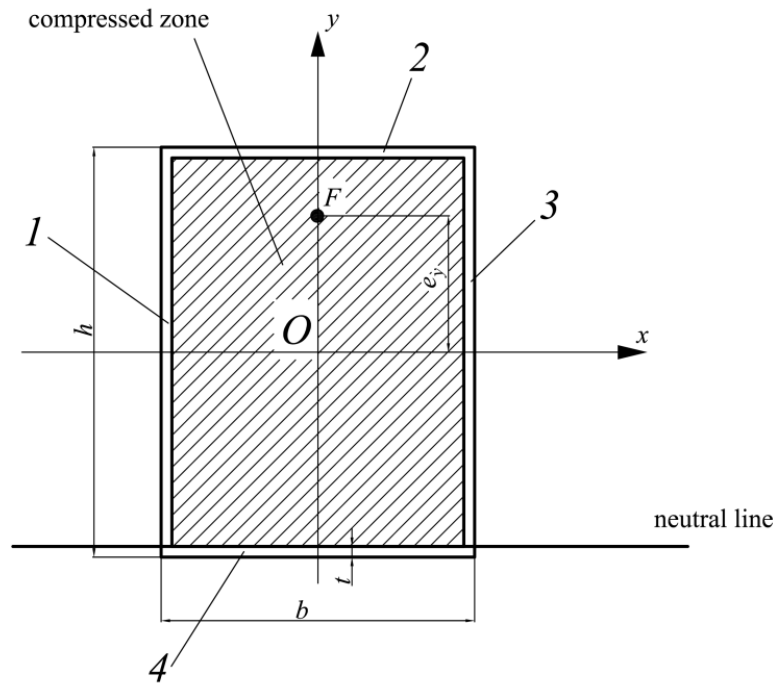


**Fig. (6).** Option 4 of the neutral line position.

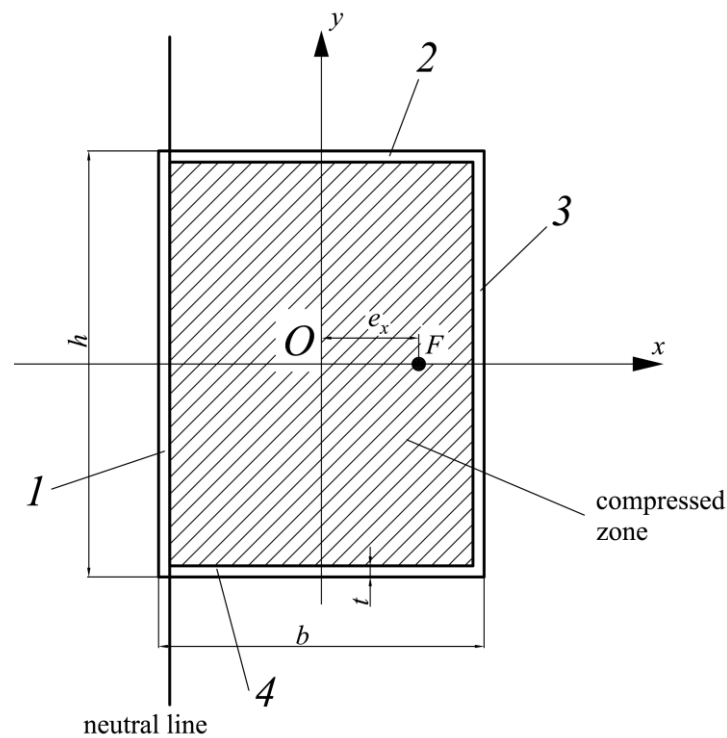
5) If one of the eccentricities of the axial force  $e_x$  is equal to zero, then a case is possible when the compressed zone of concrete covers the entire concrete core, and only side 4 of the steel pipe works in tension (Fig. 7).

6) When  $e_y = 0$  and  $e_x \neq 0$  a case is possible, when only side 1 of the steel pipe is subject to tension (Fig. 8).

7) Case of axial compression  $e_x = 0$   $e_y = 0$ .



**Fig. (7).** Option 5 of the neutral line position.



**Fig. (8).** Option 6 of the neutral line position.

Let us begin by considering option 1. The following constraints must be met with this option for distances  $y_1$  and  $y_3$  according to Fig. (3) (Eq. 1):

$$\begin{aligned} -\frac{h}{2} &\leq y_1 \leq \frac{h}{2}; \\ -\frac{h}{2} &\leq y_3 \leq \frac{h}{2}. \end{aligned} \quad (1)$$

The axial compressive force perceived by concrete is the product of the concrete compressive strength  $R_b$  and the area of the concrete core compressed zone (Eq. 2):

$$N_b = R_b \left( \frac{b \cdot h}{2} + \frac{y_1 + y_3}{2} \cdot b \right). \quad (2)$$

The axial compressive force perceived by the steel shell  $N_s$  is the product of the yield strength and the difference between the cross-sectional area of the compressed zone of the steel pipe and the tensile zone area.  $N_s$  value can be written as (Eq. 3):

$$\begin{aligned} N_s &= R_y (b \cdot t + t \cdot (h + y_1 + y_3) - b \cdot t \\ &- t \cdot \left( \frac{h}{2} - y_3 \right) - t \cdot \left( \frac{h}{2} - y_1 \right)) = 2R_y t (y_1 + y_3). \end{aligned} \quad (3)$$

The sum of the forces  $N_b$  and  $N_s$  gives the magnitude of the compressive force  $F$  (Eq. 4):

$$\begin{aligned} R_b \left( \frac{b \cdot h}{2} + \frac{y_1 + y_3}{2} \cdot b \right) \\ + 2R_y \cdot t \cdot (y_1 + y_3) = F. \end{aligned} \quad (4)$$

The bending moment about the axis  $y$ , perceived by concrete, represents the product of the compressive strength, the area of the compressed zone, and the coordinate of the compressed zone center of gravity. It is written as (Eq. 5):

$$\begin{aligned} M_{by} &= R_b \cdot \frac{1}{2} (y_3 - y_1) \cdot b \cdot \frac{1}{6} b \\ &= R_b \cdot \frac{b^2}{12} \cdot (y_3 - y_1). \end{aligned} \quad (5)$$

The bending moment about the axis  $y$ , perceived by the steel shell, is determined as follows (Eq. 6):

$$\begin{aligned} M_{sy} &= 2R_y \cdot t \cdot (y_3 - y_1) \cdot \frac{b}{2} \\ &= R_y \cdot t \cdot b \cdot (y_3 - y_1). \end{aligned} \quad (6)$$

Based on Eqs. (5 and 6), the following equilibrium condition can be written (Eq. 7):

$$\begin{aligned} M_y &= M_{by} + M_{sy} \\ &= (y_3 - y_1) \cdot b \cdot \left( R_b \cdot \frac{b}{12} + R_y \cdot t \right) \\ &= F \cdot e_x. \end{aligned} \quad (7)$$

The bending moment about the axis  $x$  perceived by concrete is calculated as follows (Eq. 8):

$$\begin{aligned} M_{bx} &= R_b \left( \frac{bh}{2} \cdot \frac{h}{4} - y_1 b \cdot \frac{y_1}{2} - \frac{1}{2} (y_3 - y_1) b \left( y_1 + \frac{1}{3} (y_3 - y_1) \right) \right) \\ &= R_b b \left( \frac{h^2}{8} - \frac{1}{6} (y_1^2 + y_1 y_3 + y_3^2) \right). \end{aligned} \quad (8)$$

The bending moment about the axis  $y$ , perceived by the steel shell, is calculated using the formula (Eq. 9):

$$\begin{aligned} M_{sx} &= R_y t \left( b \cdot \frac{h}{2} \cdot 2 + 2 \cdot \frac{h}{2} \cdot \frac{h}{4} - y_1 \cdot \frac{y_1}{2} - \right. \\ &- y_3 \cdot \frac{y_3}{2} + \left. \left( \frac{h}{2} - y_1 \right) \cdot \left( y_1 + \frac{\frac{h}{2} - y_1}{2} \right) \right. \\ &+ \left. \left( \frac{h}{2} - y_3 \right) \cdot \left( y_3 + \frac{\frac{h}{2} - y_3}{2} \right) \right) \\ &= R_y t \left( bh + \frac{h^2}{2} - y_1^2 - y_3^2 \right). \end{aligned} \quad (9)$$

Based on (Eqs. 8 and 9), the following equilibrium condition can be written:

$$\begin{aligned} R_b b \left( \frac{h^2}{8} - \frac{1}{6} (y_1^2 + y_1 y_3 + y_3^2) \right) \\ + R_y t \left( bh + \frac{h^2}{2} - y_1^2 - y_3^2 \right) = F e_y. \end{aligned} \quad (10)$$

Thus, the problem of determining the ultimate load for option 1 is reduced to three equations (Eqs. 4, 7, 10) with three unknowns  $y_1$ ,  $y_3$ ,  $F$ .

The three equations indicated can be reduced to a single equation with respect to  $F$ . To do this, we express the sum  $(y_1 + y_3)$  from Eq. (4), and we express the difference  $(y_3 - y_1)$  from Eq. (7):

$$y_1 + y_3 = \frac{F - R_b \cdot \frac{bh}{2}}{R_b \cdot \frac{b}{2} + 2R_y \cdot t}. \quad (11)$$

$$y_3 - y_1 = \frac{F \cdot e_x}{b \cdot \left( R_b \cdot \frac{b}{12} + R_y \cdot t \right)}. \quad (12)$$

Adding Eqs. (11 and 12), we obtain the formula for  $y_3$  (Eq. 13):

$$y_3 = \frac{1}{2} \left[ \frac{F \cdot e_x}{b \cdot \left( R_b \cdot \frac{b}{12} + R_y \cdot t \right)} + \frac{F - R_b \cdot \frac{bh}{2}}{R_b \cdot \frac{b}{2} + 2R_y \cdot t} \right]. \quad (13)$$

Subtracting Eqs. (12 from 11), we obtain the formula for  $y_3$ :

$$y_1 = \frac{1}{2} \left[ \frac{-F \cdot e_x}{b \cdot \left( R_b \cdot \frac{b}{12} + R_y \cdot t \right)} + \frac{F - R_b \cdot \frac{bh}{2}}{R_b \cdot \frac{b}{2} + 2R_y \cdot t} \right]. \quad (14)$$

Next, substituting Eqs. (13 and 14 into 10), we obtain a quadratic equation with respect to  $F$ . The roots of this equation must be substituted into Eqs. (13 and 14) and the fulfillment of conditions in Eq. (1) must be checked. The smaller positive value of  $F$ , at which conditions in Eq. (1) are satisfied, will correspond to the ultimate load. Failure to fulfill conditions in Eq. (1) or the absence of positive roots of the quadratic equation with respect to  $F$  indicates that the limit equilibrium is not realized according to option 1.

Option 3 (Fig. 5) is similar to option 1 (Fig. 3). The equilibrium equations for this option are written as (Eqs. 15-17):

$$R_b \left( \frac{b \cdot h}{2} + \frac{x_2 + x_4}{2} \cdot h \right) + 2R_y \cdot t \cdot (x_2 + x_4) = F; \quad (15)$$

$$(x_2 - x_4) \cdot h \cdot \left( R_b \cdot \frac{h}{12} + R_y \cdot t \right) = F \cdot e_y; \quad (16)$$

$$R_b h \left( \frac{b^2}{8} - \frac{1}{6} (x_4^2 + x_2 x_4 + x_2^2) \right) + R_y t \left( bh + \frac{b^2}{2} - x_4^2 - x_2^2 \right) = F e_x. \quad (17)$$

From Eqs. (15 and 16), values  $x_2$  and  $x_4$  can be expressed through  $F$  in the following form (Eq. 18):

$$x_2 = \frac{1}{2} \left[ \frac{F \cdot e_y}{h \cdot \left( R_b \cdot \frac{h}{12} + R_y \cdot t \right)} + \frac{F - R_b \cdot \frac{bh}{2}}{R_b \cdot \frac{h}{2} + 2R_y \cdot t} \right]; \quad (18)$$

$$x_4 = \frac{1}{2} \left[ \frac{-F \cdot e_y}{h \cdot \left( R_b \cdot \frac{h}{12} + R_y \cdot t \right)} + \frac{F - R_b \cdot \frac{bh}{2}}{R_b \cdot \frac{h}{2} + 2R_y \cdot t} \right]. \quad (19)$$

Substituting Eqs. (18 and 19 into 17), we also obtain a quadratic equation with respect to  $F$ . After finding the positive roots of the equation, they must be substituted into Eqs. (18 and 19) and the conditions must be checked (Eq. 20):

$$-\frac{b}{2} \leq x_2 \leq \frac{b}{2}; \quad (20)$$

$$-\frac{b}{2} \leq x_4 \leq \frac{b}{2}.$$

Let us consider option 2 (Fig. 4). The compressive force perceived by concrete will be written as (Eq. 21):

$$N_b = R_b \left( b \cdot h - \frac{1}{2} \cdot \left( \frac{b}{2} + x_4 \right) \left( \frac{h}{2} + y_1 \right) \right). \quad (21)$$

The axial force perceived by the steel shell is determined as follows (Eq. 22):

$$N_s = R_y \cdot t \cdot \left( h + b + \frac{h}{2} - y_1 + \frac{b}{2} - x_4 - \left( \frac{b}{2} + x_4 \right) - \left( \frac{h}{2} + y_1 \right) \right) \\ = R_y \cdot t \cdot (b + h - 2y_1 - 2x_4). \quad (22)$$

The first equilibrium equation takes the form (Eq. 23):

$$R_b \left( b \cdot h - \frac{1}{2} \cdot \left( \frac{b}{2} + x_4 \right) \left( \frac{h}{2} + y_1 \right) \right) + R_y \cdot t \cdot (b + h - 2y_1 - 2x_4) = F. \quad (23)$$

The bending moment about the axis  $x$ , perceived by concrete, is determined by the formula (Eq. 24):

$$M_{bx} = R_b \cdot \frac{1}{2} \cdot \left( \frac{h}{2} + y_1 \right) \cdot \left( \frac{b}{2} + x_1 \right) \cdot \left( \frac{2}{3} \cdot \left( \frac{h}{2} + y_1 \right) - y_1 \right) \\ = R_b \cdot \frac{1}{6} \cdot \left( \frac{h}{2} + y_1 \right) \cdot \left( \frac{b}{2} + x_1 \right) \cdot (h - y_1). \quad (24)$$

The bending moment about the axis  $x$  perceived by the steel shell is calculated as follows (Eq. 25):

$$M_{sx} = R_y t \left( \frac{bh}{2} - \left( \frac{b}{2} - x_4 \right) \frac{h}{2} + \left( \frac{h}{2} - y_1 \right) \left( y_1 + \frac{\frac{h}{2} - y_1}{2} \right) + \left( \frac{b}{2} + x_4 \right) \frac{h}{2} + \left( \frac{h}{2} + y_1 \right) \left( \frac{\frac{h}{2} + y_1}{2} - y_1 \right) \right) \\ = R_y t \cdot \left( \frac{bh}{2} + x_4 h + \frac{h^2}{4} - y_1^2 \right). \quad (25)$$

The second equilibrium equation (the sum of the internal and external moments relative to the  $x$ -axis) is written as (Eq. 26):

$$\frac{R_b}{6} \left( \frac{h}{2} + y_1 \right) \left( \frac{b}{2} + x_4 \right) (h - y_1) + R_y t \left( \frac{bh}{2} + x_4 h + \frac{h^2}{4} - y_1^2 \right) = F e_y. \quad (26)$$

The equation for the sum of moments about the  $y$ -axis has a similar form (Eq. 27):

$$\begin{aligned} & \frac{R_b}{6} \left( \frac{h}{2} + y_1 \right) \left( \frac{b}{2} + x_4 \right) (b - x_4) \\ & + R_y t \left( \frac{bh}{2} + y_1 b + \frac{b^2}{4} - x_4^2 \right) = F e_x. \end{aligned} \quad (27)$$

Thus, for option 2 (Fig. 4), the problem of determining the ultimate load is reduced to a system of three nonlinear equations (Eqs. 23, 26, 27) with respect to the variables  $y_1$ ,  $x_4$  and  $F$ . In this case, the following constraints must be satisfied for  $y_1$  and  $x_4$  (Eq. 28):

$$\begin{aligned} -\frac{h}{2} & \leq y_1 \leq \frac{h}{2}; \\ -\frac{b}{2} & \leq x_4 \leq \frac{b}{2}. \end{aligned} \quad (28)$$

The nonlinear system of equations (Eqs. 23, 26, 27) has more than one solution. The problem of determining the ultimate load at failure, as per option 2, is formulated as a nonlinear optimization problem. The objective function, which is the compressive force  $F$ , as determined by Eq. (23), must reach a minimum. The constraints are determined by Eqs. (26-28). We have implemented the search for the ultimate load in the MATLAB environment using the interior point method [39].

Option 4 (Fig. 6) is similar to option 2 (Fig. 4). This option is possible in the case of large eccentricities of the axial force. The equilibrium equations for this option are written as (Eqs. 29-31):

$$\begin{aligned} & \frac{R_b}{2} \left( \frac{b}{2} - x_2 \right) \left( \frac{h}{2} - y_3 \right) \\ & - R_y t (2y_3 + 2x_2 + h + b) = F; \end{aligned} \quad (29)$$

$$\begin{aligned} & \frac{R_b}{6} \left( \frac{b}{2} - x_2 \right) \left( \frac{h}{2} - y_3 \right) (h + y_3) \\ & + R_y t \left( \frac{h^2}{4} + \frac{bh}{2} - y_3^2 - x_2 h \right) = F e_y; \end{aligned} \quad (30)$$

$$\begin{aligned} & \frac{R_b}{6} \left( \frac{b}{2} - x_2 \right) \left( \frac{h}{2} - y_3 \right) (b + x_2) \\ & + R_y t \left( \frac{b^2}{4} + \frac{bh}{2} - x_2^2 - y_3 b \right) = F e_x. \end{aligned} \quad (31)$$

The solution of system (Eqs. 29-31), as for option 2, is performed using nonlinear optimization methods. In this case, the following constraints must be satisfied for  $x_2$  and  $y_3$  (Eq. 32):

$$\begin{aligned} -\frac{h}{2} & \leq y_3 \leq \frac{h}{2}; \\ -\frac{b}{2} & \leq x_2 \leq \frac{b}{2}. \end{aligned} \quad (32)$$

The impossibility of finding a solution that satisfies conditions (Eq. 32) or the negative value of the force  $F$  found indicates that the destruction does not occur according to option 4.

For option 5 (Fig. 7), the ultimate load is determined by the formula (Eq. 33):

$$F = R_b b h + 2 R_y t h. \quad (33)$$

An indication that option 5 is being implemented may be that, when calculating according to option 1, the values  $y_1 = y_3$  turned out to be greater than  $h/2$ .

For option 6 (Fig. 8), the formula for the ultimate load has the form (Eq. 34):

$$F = R_b b h + 2 R_y t b. \quad (34)$$

An indication that option 6 is being implemented may be that when calculating according to option 3, the values  $x_2 = x_4$  turned out to be greater than  $b/2$ .

For the case of axial compression (option 7), the formula for the ultimate load has the form (Eq. 35):

$$F = R_b b h + 2 R_y t (b + h). \quad (35)$$

### 3. RESULTS

The developed methodology was tested on experimental data for 38 samples presented in three different works [40-42]. In Fig. (8), the experimental values of the ultimate load  $N_{exp}$  are plotted along the abscissa axis, and the values  $N_{calc}$  calculated using the method proposed in this article are plotted along the ordinate axis. Most of the points are located fairly close to the straight line  $N_{exp} = N_{calc}$ . A tabular presentation of the data shown in Fig. (9) is given in Table 1. This table also presents the results of the finite element calculation  $N_{FEM}$  using the simplified method given in the paper [43], and the number of the destruction scheme (option) is indicated for each sample.

It should be noted that in recent works [41, 42], concrete compressive cube strength was given instead of the prismatic compressive strength. The following relationship (Eq. 36) was used to calculate prismatic (cylindrical) compressive strength  $R_b$  by the compressive cube strength  $R$  [44]:

$$R_b = (0.77 - 0.00125R) \cdot R. \quad (36)$$

### 4. DISCUSSION

As shown in Table 1, for samples HSS3 and HSS4, as well as HSS16 and HSS17, the same ultimate load values were obtained at different eccentricities of the axial force. This can be explained by the fact that at a small eccentricity, the neutral line can be inside the wall of the steel pipe. Since we considered the wall thickness to be small compared to the cross-sectional dimensions, this case was not considered. It turned out that for both columns, destruction occurs according to Scheme 6. It should also be noted that Uy tested two twin samples for some variants (HSS1 and HSS2, HSS8 and HSS9, HSS14 and HSS15) [40].

Statistical characteristics for the relationships  $N_{exp}/N_{calc}$  and  $N_{FEM}/N_{calc}$  are presented in Table 2.

It is evident from Table 2 that the average values of the ratios  $N_{exp}/N_{calc}$  and  $N_{FEM}/N_{calc}$  are close to one. The deviation of the values from the calculated values can be explained, in part, by the scatter of experimental data. In some cases, deviations can be explained by the presence of local loss of stability effects for the pipe wall (which leads to a decrease in the actual ultimate load compared to the calculated one). The other reason for deviations is an increase in the bearing capacity of the concrete core due to the effect of lateral compression (which leads to an increase in the actual ultimate load compared to the calculated one).

The values  $N_{FEM}$  show a smaller deviation from the values  $N_{calc}$ , since the finite element calculation excludes

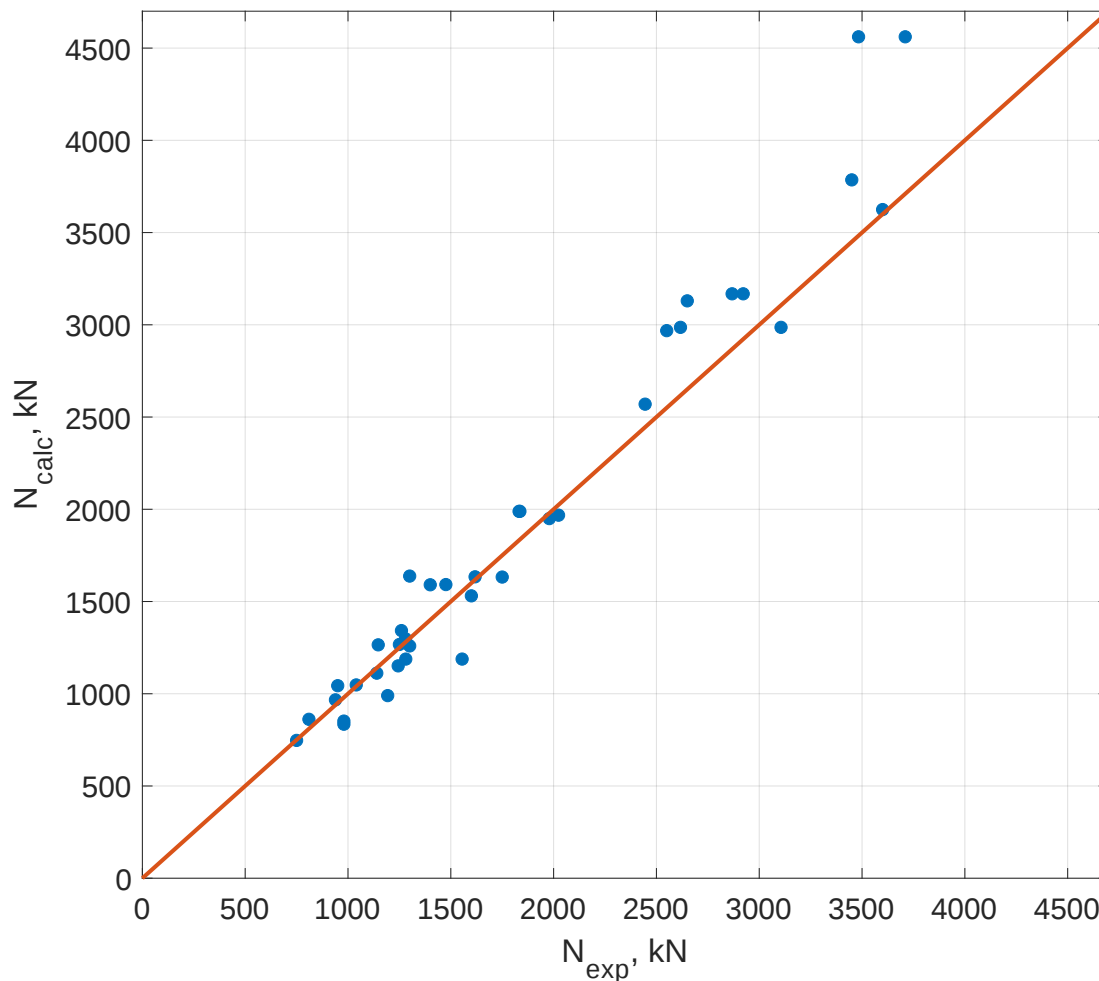
errors associated with the spread of material characteristics and the presence of random eccentricities. The correlation coefficient between the values  $N_{exp}$  and  $N_{calc}$  was 0.979, and between the values  $N_{FEM}$  and  $N_{calc}$  it was 0.983.

For the possibility to reproduce the results, we also give a numerical example of calculation for the sample Rcfst-4 from Table 1 at  $b = 0.18$  m,  $h = 0.12$  m,  $t = 3 \cdot 10^{-3}$  m,  $R_b = 4.67 \cdot 10^4$  kPa,  $R_y = 3.24 \cdot 10^5$  kPa,  $e_x = 0.036$  m,  $e_y = 0.024$  m.

To determine the ultimate load according to option 1, we substitute the initial data into Eqs. (13 and 14). As a result, we obtain Eqs. (37 and 38):

$$y_1 = 2.15 \cdot 10^{-5} F - 0.041; \quad (37)$$

$$y_3 = 1.41 \cdot 10^{-4} F - 0.041. \quad (38)$$



**Fig. (9).** Comparison of calculation results with experimental data.

Table 1. Comparison of calculation results with experimental data.

| Sample                         | $b$ , cm | $h$ , cm | $t$ , mm | $R_b$ , MPa | $R_y$ , MPa | $e_x$ , cm | $e_y$ , cm | $N_{exp}$ , kN | $N_{FEM}$ , kN | $N_{calc}$ , kN | Scheme |
|--------------------------------|----------|----------|----------|-------------|-------------|------------|------------|----------------|----------------|-----------------|--------|
| Uy, 2001 [40]                  |          |          |          |             |             |            |            |                |                |                 |        |
| HSS1                           | 11       | 11       | 5        | 28          | 750         | 0          | 0          | 1836           | 1909           | 1989            | 7      |
| HSS2                           | 11       | 11       | 5        | 28          | 750         | 0          | 0          | 1832           | 1909           | 1989            | 7      |
| HSS3                           | 11       | 11       | 5        | 30          | 750         | 1.5        | 0          | 1555           | 1400           | 1188            | 6      |
| HSS4                           | 11       | 11       | 5        | 30          | 750         | 3          | 0          | 1281           | 1127           | 1188            | 6      |
| HSS8                           | 16       | 16       | 5        | 30          | 750         | 0          | 0          | 2868           | 3097           | 3168            | 7      |
| HSS9                           | 16       | 16       | 5        | 30          | 750         | 0          | 0          | 2922           | 3097           | 3168            | 7      |
| HSS10                          | 16       | 16       | 5        | 30          | 750         | 2.5        | 0          | 2024           | 2186           | 1968            | 6      |
| HSS11                          | 16       | 16       | 5        | 30          | 750         | 5          | 0          | 1979           | 1742           | 1950            | 3      |
| HSS14                          | 21       | 21       | 5        | 32          | 750         | 0          | 0          | 3710           | 4452           | 4561            | 7      |
| HSS15                          | 21       | 21       | 5        | 32          | 750         | 0          | 0          | 3483           | 4452           | 4561            | 7      |
| HSS16                          | 21       | 21       | 5        | 32          | 750         | 2.5        | 0          | 3106           | 3417           | 2986            | 6      |
| HSS17                          | 21       | 21       | 5        | 32          | 750         | 5          | 0          | 2617           | 2826           | 2986            | 6      |
| Yang <i>et al.</i> , 2011 [41] |          |          |          |             |             |            |            |                |                |                 |        |
| Scfst-1                        | 15       | 15       | 3        | 46.7        | 324         | 0          | 0          | 1618           | 1559           | 1634            | 7      |
| Scfst-2                        | 15       | 15       | 3        | 46.7        | 324         | 1.5        | 0          | 1260           | 1260           | 1342            | 6      |
| Scfst-3                        | 15       | 15       | 3        | 46.7        | 324         | 3          | 0          | 1244           | 1057           | 1151            | 3      |
| Scfst-4                        | 15       | 15       | 3        | 46.7        | 324         | 1.5        | 1.5        | 1280           | 1195           | 1298            | 2      |
| Scfst-5                        | 15       | 15       | 3        | 46.7        | 324         | 3          | 3          | 1193           | 925            | 990             | 2      |
| Rcfst-1                        | 18       | 12       | 3        | 46.7        | 324         | 0          | 0          | 1476           | 1517           | 1592            | 7      |
| Rcfst-2                        | 18       | 12       | 3        | 46.7        | 324         | 3.6        | 0          | 1140           | 1020           | 1112            | 3      |
| Rcfst-3                        | 18       | 12       | 3        | 46.7        | 324         | 1.8        | 1.2        | 1147           | 1160           | 1265            | 2      |
| Rcfst-4                        | 18       | 12       | 3        | 46.7        | 324         | 3.6        | 2.4        | 939            | 900            | 967             | 2      |

(Table 1) contd.....

| Sample                  | b, cm | h, cm | t, mm | $R_b$ , MPa | $R_y$ , MPa | $e_x$ , cm | $e_y$ , cm | $N_{exp}$ , kN | $N_{FEM}$ , kN | $N_{calc}$ , kN | Scheme |
|-------------------------|-------|-------|-------|-------------|-------------|------------|------------|----------------|----------------|-----------------|--------|
| X. Qu et al., 2013 [42] |       |       |       |             |             |            |            |                |                |                 |        |
| PYA-1                   | 15    | 10    | 4.065 | 30.7        | 235         | 1          | 0          | 750            | 735            | 747             | 6      |
| PYA-2                   | 15    | 10    | 4.065 | 52.0        | 235         | 1.5        | 0          | 1040           | 936            | 1048            | 3      |
| PYA-3                   | 15    | 10    | 4.065 | 41.0        | 235         | 2          | 0          | 810            | 745            | 862             | 3      |
| PYA-4                   | 20    | 15    | 4.433 | 41.0        | 235         | 2          | 0          | 1750           | 1470           | 1633            | 3      |
| PYA-5                   | 20    | 15    | 4.433 | 30.7        | 235         | 3          | 0          | 1250           | 1100           | 1267            | 3      |
| PYA-6                   | 20    | 15    | 4.433 | 52.0        | 235         | 4          | 0          | 1400           | 1372           | 1591            | 3      |
| PYA-7                   | 30    | 20    | 5.73  | 52.0        | 345         | 5          | 0          | 3450           | 3243           | 3786            | 3      |
| PYA-8                   | 30    | 20    | 5.73  | 41.0        | 345         | 6          | 0          | 2650           | 2703           | 3130            | 3      |
| PYA-9                   | 30    | 20    | 5.73  | 30.7        | 345         | 7          | 0          | 2445           | 2152           | 2570            | 3      |
| PYB-1                   | 15    | 10    | 4.065 | 30.7        | 235         | 0.832      | 0.555      | 980            | 804            | 835             | 2      |
| PYB-2                   | 15    | 10    | 4.065 | 52.0        | 235         | 1.248      | 0.832      | 950            | 855            | 1044            | 2      |
| PYB-3                   | 15    | 10    | 4.065 | 41.0        | 235         | 1.664      | 1.109      | 980            | 921            | 852             | 2      |
| PYB-4                   | 20    | 15    | 4.433 | 41.0        | 235         | 1.6        | 1.2        | 1300           | 1456           | 1638            | 2      |
| PYB-5                   | 20    | 15    | 4.433 | 30.7        | 235         | 2.4        | 1.8        | 1300           | 1066           | 1259            | 2      |
| PYB-6                   | 20    | 15    | 4.433 | 52.0        | 235         | 3.2        | 2.4        | 1600           | 1376           | 1531            | 2      |
| PYB-7                   | 30    | 20    | 5.73  | 52.0        | 345         | 3.841      | 3.201      | 3600           | 2952           | 3625            | 2      |
| PYB-8                   | 30    | 20    | 5.73  | 41.0        | 345         | 4.609      | 3.841      | 2550           | 2601           | 2968            | 2      |

Table 2. Statistical characteristics for the relationships  $N_{exp}/N_{calc}$  and  $N_{FEM}/N_{calc}$ .

| Value              | Average | Min   | Max   | Standard Deviation | Coefficient of Variation, % |
|--------------------|---------|-------|-------|--------------------|-----------------------------|
| $N_{exp}/N_{calc}$ | 0.978   | 0.764 | 1.309 | 0.113              | 11.5                        |
| $N_{FEM}/N_{calc}$ | 0.936   | 0.814 | 1.178 | 0.0825             | 8.8                         |

Let us further substitute Eqs. (37 and 38 into 10). As a result, we obtain a quadratic equation with respect to  $F$  (Eq. 39):

$$-5.26 \cdot 10^{-5} F^2 + 0.017 F + 22.28 = 0. \quad (39)$$

The roots of this equation are:  $F_1 = -508.75$  kN and  $F_2 = 832.52$  kN. Substituting the positive root of Eqs. (39 into 37 and 38), we obtain  $y_1 = -0.023$  m and  $y_3 = 0.0764$  m. Since  $y_3 > h/2$  the destruction does not occur according to option 1.

Let us now consider option 3, the destruction option. Substituting the initial data into Eqs. (18-19), we obtain Eqs. (40 and 41):

$$x_2 = 1.75 \cdot 10^{-4} F - 0.0531; \quad (40)$$

$$x_4 = 3.58 \cdot 10^{-5} F - 0.0531. \quad (41)$$

Substituting Eqs. (40 and 41 into 17), we obtain the following quadratic equation (Eq. 42):

$$-6.66 \cdot 10^{-5} F^2 + 0.0171 F + 35.54 = 0. \quad (42)$$

This equation has roots  $F_1 = -613$  kN and  $F_2 = 871$  kN. Substituting  $F = 871$  kN into Eqs. (40 and 41) yield  $x_2$  m and  $x_4$  m. Since  $x_2 > b/2$ , the destruction does not occur according to option 3.

Next, we proceed to option 2, the destruction option. Determining the ultimate load according to this option, in

addition to the Optimization Toolbox package of the MATLAB environment, is also available from Microsoft Excel when using the Solver add-in.

Fig. (10) shows a screenshot from the Microsoft Excel Online program. Cells B1:B7 represent the initial data. Cells B9:B10 are intended for the variables  $y_1, x_4$ . The coordinates of the initial search point are entered into these cells, which we take to be equal to  $[h/4; b/4]$ . Cell B12 represents the objective function, which is determined by Eq. (23). Constraints "constraint1" and "constraint2" are determined based on Eqs. (26, 27). Fig. (11) illustrates all the constraints for this optimization problem, as well as the solution found. The solution was found, and all constraints were satisfied. The ultimate load according to option 2 was 967 kN, and the parameters  $y_1$  and  $x_4$ , which determine the position of the neutral line, were equal to 0.0277 and 0.0238 m, respectively.

Let us now consider the destruction option 4. The solution is performed similarly to option 2. For this variant, the solver was unable to find a possible solution (Fig. 12), which indicates the impossibility of destruction according to option 4.

Thus, finally, according to the calculation results, destruction occurs according to option 2 at the ultimate load of  $F_{ult} = 967$  kN. The experimental value of the ultimate load is 939 kN, which differs by 2.9% from the theoretical value.

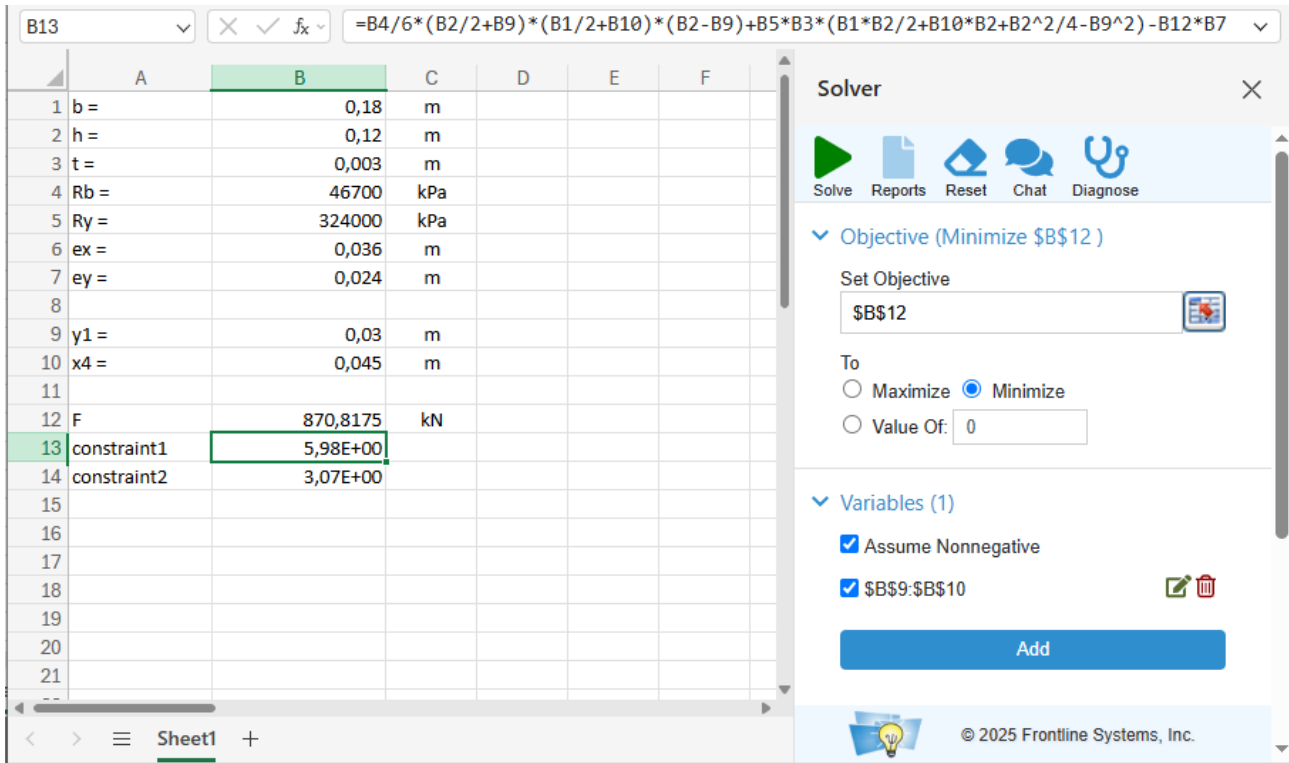


Fig. (10). Screenshot from the Microsoft Excel Online program.

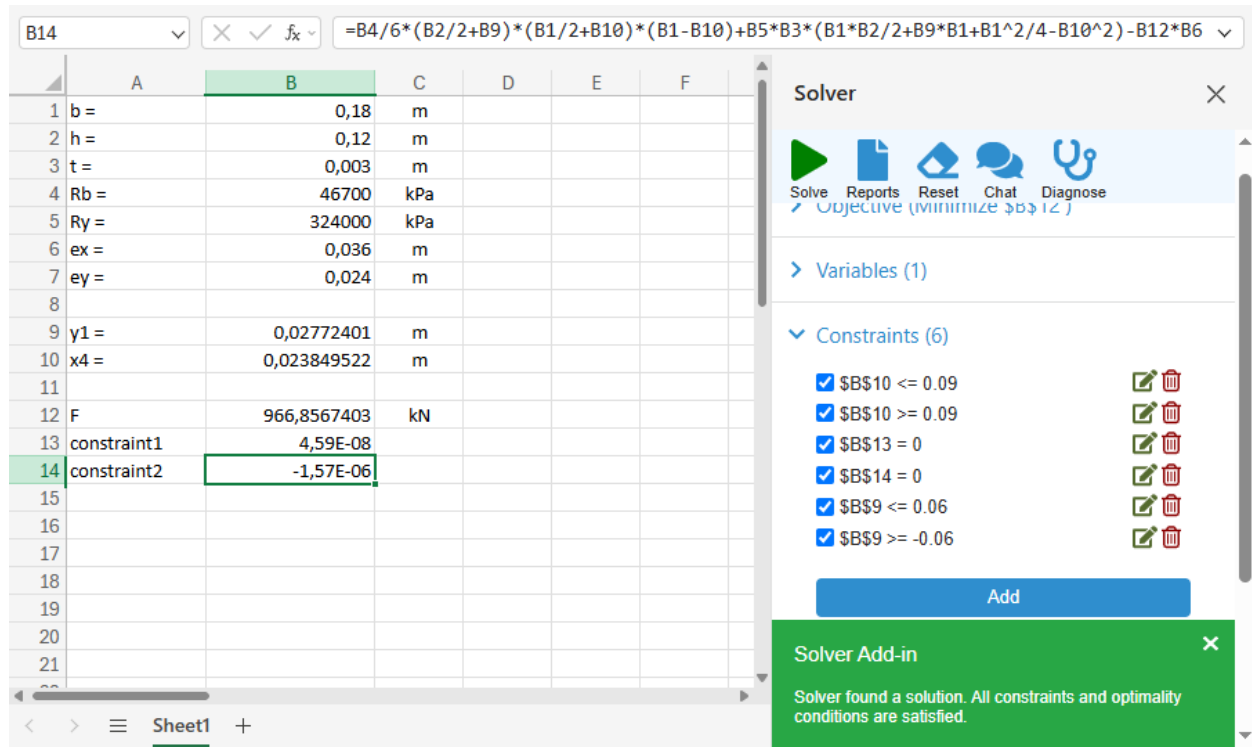


Fig. (11). Constraints in the optimization problem and the result of finding a solution.

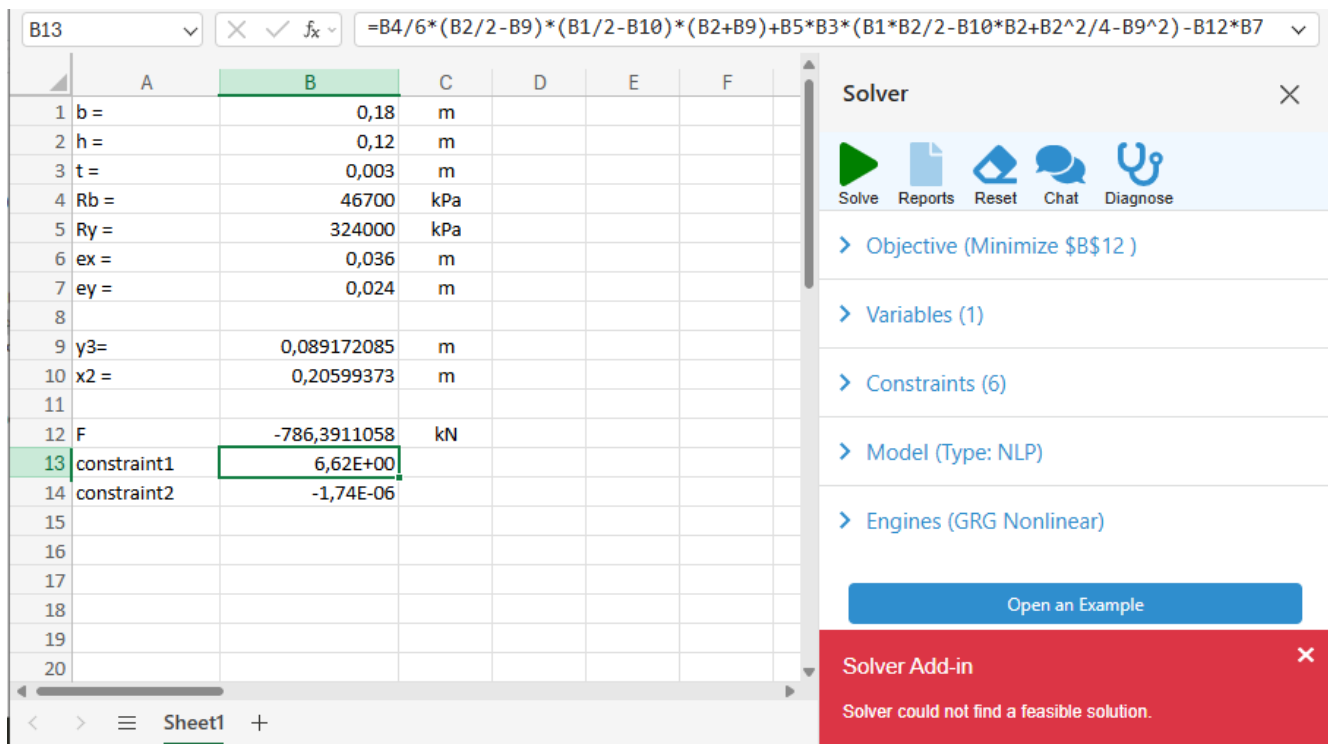


Fig. (12). Result of searching for a solution for destruction according to option 4.

## CONCLUSION

An analytical model is proposed for determining the bearing capacity of eccentrically compressed rectangular CFST columns in the presence of axial force eccentricities in two planes. The developed model is based on the limit equilibrium method. All possible variants of the compressed zone location in the cross section are considered, and for the considered variants, resolving equations are obtained that allow determining the ultimate load. For two possible failure schemes, the problem is reduced to a quadratic equation related to the ultimate load. For the other two schemes, the calculation is simplified to solving a system of three nonlinear equations, which can be performed using a publicly available tool such as Microsoft Excel Online.

The calculation method was tested on the results of experiments for 38 samples presented in three different works. The average value of the experimental ultimate load to the calculated ultimate load ratio is close to one, and the correlation coefficient between the experimental and calculated values of the ultimate load was 0.979. The calculation results obtained using the proposed analytical model are also very close to those of the finite element analysis. This suggests the potential application of the proposed model in engineering practice for preliminary bearing capacity assessments of rectangular CFST columns. To facilitate the reproduction of the results and their application in engineering practice, a numerical example of the calculation was also provided.

## STUDY LIMITATIONS

The limitations of the model include that it does not take into account additional eccentricities of the axial force caused by the deflection of the element. The model is applicable for short columns whose slenderness ratio (the ratio of the calculated length to the minimum radius of gyration for reduced cross-section) does not exceed 14. Additionally, the proposed model overlooks the effects of local stability loss in the pipe wall, the work of the tensile zone in concrete, and the increase in the bearing capacity of the concrete core resulting from lateral compression. The confinement effect can be taken into account by adjusting the design strength of the concrete and steel pipe. Considering the effect of concrete lateral compression by the steel tube in the proposed model is a prospect for our further research.

## AUTHORS' CONTRIBUTIONS

The authors confirm their contribution to the paper as follows: A.C.: Study conception and design; V.T.: Analysis and interpretation of results; S.A.Z.: Draft manuscript. All authors reviewed the results and approved the final version of the manuscript.

## LIST OF ABBREVIATIONS

|       |                                    |
|-------|------------------------------------|
| $R_b$ | = Compressive strength of concrete |
| $R_y$ | = Yield strength of the steel      |
| $b$   | = Cross-section width              |
| $h$   | = Cross-section height             |

|                      |                                                                |
|----------------------|----------------------------------------------------------------|
| $e_x, e_y$           | = Axial force eccentricities along the x and y axes            |
| $t$                  | = Thickness of the rectangular steel profile pipe              |
| $x_2, x_4, y_1, y_3$ | = Distances determining the position of the neutral line       |
| $F$                  | = Compressive force                                            |
| $N_b$                | = Axial compressive force perceived by concrete                |
| $N_s$                | = Axial compressive force perceived by steel                   |
| $M_{bx}, M_{by}$     | = The concrete perceives bending moments in the x and y axes   |
| $M_{sx}, M_{sy}$     | = Bending moments in the x and y axes perceived by steel       |
| $M_x, M_y$           | = Total bending moments in the x and y axes                    |
| $N_{exp}$            | = Experimental values of the ultimate load                     |
| $N_{calc}$           | = Analytical values of the ultimate load                       |
| $N_{FEM}$            | = Ultimate load values calculated by the finite element method |

## CONSENT FOR PUBLICATION

Not applicable.

## AVAILABILITY OF DATA AND MATERIALS

The data and supportive information are available within the article.

## FUNDING

None.

## CONFLICT OF INTEREST

The authors declare no conflict of interest, financial or otherwise.

## ACKNOWLEDGEMENTS

Declared none.

## REFERENCES

- [1] H. Nakahara, K. Uchida, and Y. Yanai, "Test and analysis for shearing behavior of circular CFST columns", *Buildings*, vol. 14, no. 12, p. 3871, 2024. [http://dx.doi.org/10.3390/buildings14123871]
- [2] Y. Yang, J. Xue, Z. Liu, J. Wang, and X. Wang, "Seismic performance of precast frame with RC beam and spliced CFST column under cyclic loading", *Eng. Struct.*, vol. 335, p. 120363, 2025. [http://dx.doi.org/10.1016/j.engstruct.2025.120363]
- [3] R. Lu, H. Hou, C. Zhang, Z. Zhou, J. Wang, N. Wang, and D. Wang, "Seismic behavior of CFST-enhanced superimposed RC shear walls", *Constr. Build. Mater.*, vol. 472, p. 140875, 2025. [http://dx.doi.org/10.1016/j.conbuildmat.2025.140875]
- [4] D.F. Du, J. Wang, and C. Su, "Post-earthquake safety and resilience of concrete bridges with debonded high-strength reinforced concrete encased-and-filled steel tubular columns", *Research Square*, pp. 1-6, 2022. [http://dx.doi.org/10.21203/rs.3.rs-1464559/v1]
- [5] Y.C. Pan, G.H. Wang, and K. Xiang, "Overview of research

- progress for concrete-filled steel tubular columns after exposure to fire", *Appl. Mech. Mater.*, vol. 638-640, pp. 197-201, 2014.  
[http://dx.doi.org/10.4028/www.scientific.net/AMM.638-640.197]
- [6] T. Du, F. Liu, H. Yang, and K. Peng, "Fire behaviour of axially loaded high-strength concrete-filled circular high-strength steel tubular columns", *Eng. Struct.*, vol. 328, p. 119781, 2025.  
[http://dx.doi.org/10.1016/j.engstruct.2025.119781]
  - [7] G.Q. Wei, W.D. Wang, K. Zhou, and W.J. Mao, "Experimental and numerical investigation of circular concrete-filled steel tubular columns subjected to post-earthquake fires", *Eng. Struct.*, vol. 332, p. 120008, 2025.  
[http://dx.doi.org/10.1016/j.engstruct.2025.120008]
  - [8] C. Song, Y.B. Wang, G.Q. Li, and J.Y.R. Liew, "Influence of slenderness on confining effect of axially loaded circular CFST columns with high-strength materials", *Eng. Struct.*, vol. 333, p. 120041, 2025.  
[http://dx.doi.org/10.1016/j.engstruct.2025.120041]
  - [9] X. Zhou, "Application of steel-tubed concrete structures in high-rise buildings", *Inter. J. High Rise Build.*, vol. 8, no. 3, pp. 161-167, 2019.  
[http://dx.doi.org/10.21022/IJHRB.2019.8.3.161]
  - [10] S. Morino, "Recent developments on concrete-filled steel tube members in japan", *Proceedings of the International Conference on Advances in Structural Engineering* 2002.  
[http://dx.doi.org/10.1061/40616(281)56]
  - [11] K. Klöppel, and W. Goder, "Traglastversuche mit ausbetonierten Stahlrohren und Aufstellung einer Bemessungsformel", *Stahlbau*, vol. 26, no. 1, pp. 1-10, 1957.
  - [12] B. Uy, Z. Tao, and L.H. Han, "Behaviour of short and slender concrete-filled stainless steel tubular columns", *J. Construct. Steel Res.*, vol. 67, no. 3, pp. 360-378, 2011.  
[http://dx.doi.org/10.1016/j.jcsr.2010.10.004]
  - [13] C.D. Goode, "Composite columns—1819 tests on concrete-filled steel tube columns compared with Eurocode 4", *Struct. Eng.*, vol. 86, no. 16, pp. 33-38, 2008.
  - [14] Z. Tao, U.Y. Brian, L.H. Han, and S.H. He, "Design of concrete-filled steel tubular members according to the Australian Standard AS 5100 model and calibration", *Australian J. Struct. Eng.*, vol. 8, no. 3, pp. 197-214, 2008.  
[http://dx.doi.org/10.1080/13287982.2008.11464998]
  - [15] R. Leon, T. Perea, J. Hajjar, and M.M. Denavit, "Concrete-filled tubes columns and beam-columns: A database for the AISC 2005 and 2010 specifications", Available from: [https://www.researchgate.net/publication/261179847\\_Concrete-Filled\\_Tubes\\_Columns\\_and\\_Beam-Columns\\_A\\_Database\\_for\\_the\\_AISC\\_2005\\_and\\_2010\\_Specifications](https://www.researchgate.net/publication/261179847_Concrete-Filled_Tubes_Columns_and_Beam-Columns_A_Database_for_the_AISC_2005_and_2010_Specifications)
  - [16] Q. Yu, Z. Tao, and Y.X. Wu, "Experimental behaviour of high performance concrete-filled steel tubular columns", *Thin-walled Struct.*, vol. 46, no. 4, pp. 362-370, 2008.  
[http://dx.doi.org/10.1016/j.tws.2007.10.001]
  - [17] T. Ekmekyapar, and B.J.M. AL-Eliwi, "Experimental behaviour of circular concrete filled steel tube columns and design specifications", *Thin-walled Struct.*, vol. 105, pp. 220-230, 2016.  
[http://dx.doi.org/10.1016/j.tws.2016.04.004]
  - [18] A.H. Varma, J.M. Ricles, R. Sause, and L.W. Lu, "Experimental behavior of high strength square concrete-filled steel tube beam-columns", *J. Struct. Eng.*, vol. 128, no. 3, pp. 309-318, 2002.  
[http://dx.doi.org/10.1061/(ASCE)0733-9445(2002)128:3(309)]
  - [19] D.M. Lue, J.L. Liu, and T. Yen, "Experimental study on rectangular CFT columns with high-strength concrete", *J. Construct. Steel Res.*, vol. 63, no. 1, pp. 37-44, 2007.  
[http://dx.doi.org/10.1016/j.jcsr.2006.03.007]
  - [20] D. Hernández-Figueirido, M.L. Romero, J.L. Bonet, and J.M. Montalvá, "Influence of slenderness on high-strength rectangular concrete-filled tubular columns with axial load and nonconstant bending moment", *J. Struct. Eng.*, vol. 138, no. 12, pp. 1436-1445, 2012.  
[http://dx.doi.org/10.1061/(ASCE)ST.1943-541X.0000590]
  - [21] J.M. Portolés, M.L. Romero, J.L. Bonet, and F.C. Filippou, "Experimental study of high strength concrete-filled circular tubular columns under eccentric loading", *J. Construct. Steel Res.*, vol. 67, no. 4, pp. 623-633, 2011.  
[http://dx.doi.org/10.1016/j.jcsr.2010.11.017]
  - [22] X. Zhou, T. Mou, H. Tang, and B. Fan, "Experimental study on ultrahigh strength concrete filled steel tube short columns under axial load", *Adv. Mater. Sci. Eng.*, vol. 2017, pp. 1-9, 2017.  
[http://dx.doi.org/10.1155/2017/8410895]
  - [23] Z. Tao, L.H. Han, and Z.B. Wang, "Experimental behaviour of stiffened concrete-filled thin-walled hollow steel structural (HSS) stub columns", *J. Construct. Steel Res.*, vol. 61, no. 7, pp. 962-983, 2005.  
[http://dx.doi.org/10.1016/j.jcsr.2004.12.003]
  - [24] Z. Tao, L.H. Han, and D.Y. Wang, "Experimental behaviour of concrete-filled stiffened thin-walled steel tubular columns", *Thin-walled Struct.*, vol. 45, no. 5, pp. 517-527, 2007.  
[http://dx.doi.org/10.1016/j.tws.2007.04.003]
  - [25] B. Young, and E. Ellobody, "Experimental investigation of concrete-filled cold-formed high strength stainless steel tube columns", *J. Construct. Steel Res.*, vol. 62, no. 5, pp. 484-492, 2006.  
[http://dx.doi.org/10.1016/j.jcsr.2005.08.004]
  - [26] Y. Du, Z. Chen, Y.B. Wang, and J.Y. Richard Liew, "Ultimate resistance behavior of rectangular concrete-filled tubular beam-columns made of high-strength steel", *J. Construct. Steel Res.*, vol. 133, pp. 418-433, 2017.  
[http://dx.doi.org/10.1016/j.jcsr.2017.02.024]
  - [27] Y. Du, Z. Chen, and Y. Yu, "Behavior of rectangular concrete-filled high-strength steel tubular columns with different aspect ratio", *Thin-walled Struct.*, vol. 109, pp. 304-318, 2016.  
[http://dx.doi.org/10.1016/j.tws.2016.10.005]
  - [28] B. Cao, L. Zhu, X. Jiang, and C. Wang, "An investigation of compression bearing capacity of concrete-filled rectangular stainless steel tubular columns under axial load and eccentric axial load", *Sustainability*, vol. 14, no. 14, p. 8946, 2022.  
[http://dx.doi.org/10.3390/su14148946]
  - [29] H.F. Isleem, P. Jagadesh, S. Qaidi, F. Althoei, C. Rahmawati, H.M. Najm, and M.M.S. Sabri, "Finite element and theoretical investigations on PVC-CFRP confined concrete columns under axial compression", *Front. Mater.*, vol. 9, p. 1055397, 2022.  
[http://dx.doi.org/10.3389/fmats.2022.1055397]
  - [30] Y. Xu, H. Tang, J. Chen, Y. Jia, and R. Liu, "Numerical analysis of CFRP-confined concrete-filled stainless steel tubular stub columns under axial compression", *J. Build. Eng.*, vol. 37, p. 102130, 2021.  
[http://dx.doi.org/10.1016/j.job.2020.102130]
  - [31] M. Khan, B. Uy, Z. Tao, and F. Mashiri, "Behaviour and design of short high-strength steel welded box and concrete-filled tube (CFT) sections", *Eng. Struct.*, vol. 147, pp. 458-472, 2017.  
[http://dx.doi.org/10.1016/j.engstruct.2017.06.016]
  - [32] G. Li, B. Chen, Z. Yang, and Y. Feng, "Experimental and numerical behaviour of eccentrically loaded high strength concrete filled high strength square steel tube stub columns", *Thin-walled Struct.*, vol. 127, pp. 483-499, 2018.  
[http://dx.doi.org/10.1016/j.tws.2018.02.024]
  - [33] X. Ke, H. Wei, L. Yang, and H. Sun, "Analysis and calculation method for concrete-encased CFST columns under eccentric compression", *J. Construct. Steel Res.*, vol. 206, p. 107927, 2023.  
[http://dx.doi.org/10.1016/j.jcsr.2023.107927]
  - [34] Z. Tao, and L. H. Han, "Hysteretic behaviors of concrete-filled steel SHS beam-columns", In: S.L. Chan, J.G. Teng, K.F. Chung, Eds., *Advances in Steel Structures (ICASS '02)*, Elsevier: Amsterdam, Netherlands, 2002, pp. 591-598.  
[http://dx.doi.org/10.1016/B978-008044017-0/50069-X]
  - [35] M. Denavit, J. Hajjar, and R. Leon, "Advanced analysis and seismic design of concrete-filled steel tube structures", *ASCE Structures Congress 2015* 2015, pp. 823-834.  
[http://dx.doi.org/10.1061/9780784479117.083]
  - [36] B.L. Lai, W.K. Tan, Q.T. Feng, and A. Venkateshwaran, "Numerical parametric study on the uniaxial and biaxial compressive behavior of H-shaped steel reinforced concrete composite beam-columns", *Adv. Struct. Eng.*, vol. 25, no. 13, pp.

- 2641-2661, 2022.  
[<http://dx.doi.org/10.1177/13694332221105333>]
- [37] P. Foraboschi, "Optimal design of seismic resistant RC columns", *Materials*, vol. 13, no. 8, p. 1919, 2020.  
[<http://dx.doi.org/10.3390/ma13081919>] [PMID: 32325808]
- [38] P. Foraboschi, "Lateral load-carrying capacity of steel columns with fixed-roller end supports", *J. Build. Eng.*, vol. 26, p. 100879, 2019.  
[<http://dx.doi.org/10.1016/j.jobbe.2019.100879>]
- [39] A.S. Chepurnenko, V.S. Turina, and V.F. Akopyan, "Optimization of rectangular and box sections in oblique bending and eccentric compression", *Construct. Mat. prod.*, vol. 6, no. 5, p. 2, 2023.  
[<http://dx.doi.org/10.58224/2618-7183-2023-6-5-2>]
- [40] B. Uy, "Strength of short concrete filled high strength steel box columns", *J. Construct. Steel Res.*, vol. 57, no. 2, pp. 113-134, 2001.  
[[http://dx.doi.org/10.1016/S0143-974X\(00\)00014-6](http://dx.doi.org/10.1016/S0143-974X(00)00014-6)]
- [41] Y.F. Yang, and L.H. Han, "Behaviour of concrete filled steel tubular (CFST) stub columns under eccentric partial compression", *Thin-walled Struct.*, vol. 49, no. 2, pp. 379-395, 2011.  
[<http://dx.doi.org/10.1016/j.tws.2010.09.024>]
- [42] X. Qu, Z. Chen, and G. Sun, "Experimental study of rectangular CFST columns subjected to eccentric loading", *Thin-walled Struct.*, vol. 64, pp. 83-93, 2013.  
[<http://dx.doi.org/10.1016/j.tws.2012.12.006>]
- [43] A. Chepurnenko, B. Yazyev, B. Meskhi, A. Beskopylny, K. Khashkhozhhev, and V. Chepurnenko, "Simplified 2D finite element model for calculation of the bearing capacity of eccentrically compressed concrete-filled steel tubular columns", *Appl. Sci.*, vol. 11, no. 24, p. 11645, 2021.  
[<http://dx.doi.org/10.3390/app112411645>]
- [44] S.V. Litvinov, B.M. Yazyev, V.V. Kuznetsov, N.V. Belyugin, and A.A. Avakov, "Study of the concordance between various concrete deformation models and experimental data for uniaxial compression cases", *Construct. Mat. Prod.*, vol. 7, no. 5, p. 6, 2024.  
[<http://dx.doi.org/10.58224/2618-7183-2024-7-5-6>]